Homework 7 MTH 3210 Probability and Statistics Due Thu., Apr. 18

Unless stated otherwise, you must show your work to receive full credit.

| Read These Sections of the Book | Then Do These Problems |
|---------------------------------|---------------------------|
| 4.4 | Problem 1 (below), 59, 61 |
| 5.1 (Optional) | |
| 5.2 (Optional) | |
| 5.3 | Just read this section |
| 5.4 | 46, 47, 50, 51 |

1. Let

X = The time between two successive arrivals at the drive-up window of a local bank.

Suppose X has the **pdf** (an *exponential distribution*)

$$f(x) = \begin{cases} 2e^{-2x} & \text{for } x \ge 0\\ 0 & \text{otherwise} \end{cases}$$

A graph of the pdf is below.



Compute the following.

- (a) $P(X \le 4)$.
- (b) $P(2 \le X \le 5)$.
- (c) The **expected value** of the time between two successive arrivals. **Hint**: The integral $\int 2xe^{-2x} dx$ can be evaluated using *integration by parts*.