

# MTH 3220 R Notes 4

## 4 Higher Dimensional Arrays

### 4.1 Creating and Examining Arrays

- An **array** is like a matrix, but it can have more than two dimensions (e.g. it can have rows, columns, and layers).
- Here are some useful functions for creating and examining arrays:

```
array()          # Create an array, from a vector, with dimensions
                  # specified by the argument dim
dim()            # Returns the dimensions of an array
is.array()      # Indicates whether or not an object is an array
```

- Here's a three dimensional array. It has 3 rows, 3 columns, and 2 layers:

```
x <- array(1:18, dim = c(3, 3, 2))
x
## , , 1
##
##      [,1] [,2] [,3]
## [1,]    1    4    7
## [2,]    2    5    8
## [3,]    3    6    9
##
## , , 2
##
##      [,1] [,2] [,3]
## [1,]   10   13   16
## [2,]   11   14   17
## [3,]   12   15   18
##
dim(x)
## [1] 3 3 2
##
is.array(x)
## [1] TRUE
```

- Note that R fills the array one layer at a time, column by column within each layer.
- We can add names to the dimensions of an array (or get the names if they already exist) using:

```
dimnames()      # View the names of an array's dimensions or assign
                # names via a list of character vectors
```

- For example, below we create an array `TempsArray` containing temperatures ( $^{\circ}\text{K}$ ) recorded in the northern hemisphere at four longitudes (rows), three latitudes (columns), and three months (layers), and we use `dimnames()` to add names to the three dimensions of the array:

```
TempsVec <- c(273, 239, 251, 236, 284, 260, 278, 257, 305, 299, 299, 288,
             270, 260, 258, 247, 291, 287, 279, 274, 314, 302, 299, 292, 279, 279, 273,
             277, 297, 301, 284, 288, 309, 301, 301, 292)

TempsArray <- array(TempsVec, dim = c(4, 3, 3))

dimnames(TempsArray) <- list(
  Long = c("0", "90", "180", "270"),
  Lat  = c("75", "45", "15"),
  Month = c("Jan", "Apr", "Jul"))
```

```
TempsArray

## , , Month = Jan
##
##      Lat
## Long  75  45  15
##  0    273 284 305
##  90   239 260 299
## 180   251 278 299
## 270   236 257 288
##
## , , Month = Apr
##
##      Lat
## Long  75  45  15
##  0    270 291 314
##  90   260 287 302
## 180   258 279 299
## 270   247 274 292
##
## , , Month = Jul
##
##      Lat
## Long  75  45  15
##  0    279 297 309
##  90   279 301 301
## 180   273 284 301
## 270   277 288 292
```

## 4.2 Array Indexing Using [ ]

- We access array elements (rows, columns, layers, etc.) using square brackets:

```
[ , , ] # Access array elements via their dimension indices (row,
# column, layer, etc.) separated by commas
```

- For example, using the `TempsArray` array from above, to get the value in the 2nd row, 3rd column, and 1st layer, type:

```
TempsArray[2, 3, 1] # Returns the value in the 2nd row, 3rd
# column, first layer of the array
```

```
## [1] 299
```

To get all the values in the 2nd row and 3rd column, type:

```
TempsArray[2, 3, ] # Returns a vector containing the values in
# the 2nd row and 3rd column of the array
```

```
## Jan Apr Jul
## 299 302 301
```

and to all get the values in the 1st layer, type:

```
TempsArray[, , 1] # Returns a matrix containing the values in
# the 1st layer of the array
```

```
##      Lat
## Long  75  45  15
##   0  273 284 305
##   90  239 260 299
##  180  251 278 299
##  270  236 257 288
```

## Section 4.2 Exercises

**Exercise 1** Here's the `TempsArray` array again (as created above):

```

TempsArray
## , , Month = Jan
##
##      Lat
## Long  75  45  15
##   0  273 284 305
##   90  239 260 299
##  180  251 278 299
##  270  236 257 288
##
## , , Month = Apr
##
##      Lat
## Long  75  45  15
##   0  270 291 314
##   90  260 287 302
##  180  258 279 299
##  270  247 274 292
##
## , , Month = Jul
##
##      Lat
## Long  75  45  15
##   0  279 297 309
##   90  279 301 301
##  180  273 284 301
##  270  277 288 292

```

Guess what the results of each of the following will be, then check your answers (after creating the array using the commands given in Subsection 4.1).

a) `TempsArray[3, 1, 2]`

b) `TempsArray[, , 3]`

c) `TempsArray[1, , ]`

## 5 Lists

### 5.1 Creating and Examining Lists

- **Lists** are like vectors, but their elements can be *heterogeneous* (not all the same type). In fact, their elements can be *any R objects*. They're used to bundle objects together under one name.
- Lists are created and examined using:

```

list()           # Create a list
length()        # Returns the number of elements in a list

```

```
is.list()      # Indicates whether or not an object is a list
str()         # Describes the structure of a list
```

- Here's a simple list `y` that stores numeric, "character", and "logical" values:

```
y <- list(2, "a", TRUE)
y
## [[1]]
## [1] 2
##
## [[2]]
## [1] "a"
##
## [[3]]
## [1] TRUE

is.list(y)

## [1] TRUE
```

Notice that the indices of the list elements are printed in double square brackets `[[ ]]`.

- Here's a list `x` whose elements are vectors and a matrix. Notice that we assign names (`x1`, `x2`, and `x3`) to the list elements when creating the list:

```
x <- list(x1 = c(1, 2, 3),
         x2 = c("a", "b", "c"),
         x3 = matrix(1:4, nrow = 2, ncol = 2))
x
## $x1
## [1] 1 2 3
##
## $x2
## [1] "a" "b" "c"
##
## $x3
##      [,1] [,2]
## [1,]    1    3
## [2,]    2    4
```

When list elements have names (like `x1`, `x2`, and `x3` above), R prints the names preceded by a dollar sign `$`.

- `length()` tells how many elements are contained in a list:

```
length(x)

## [1] 3
```

- `str()` tells us the "structure" of the list:

```
str(x)

## List of 3
## $ x1: num [1:3] 1 2 3
## $ x2: chr [1:3] "a" "b" "c"
## $ x3: int [1:2, 1:2] 1 2 3 4
```

The output above says that `x` is a list with three elements: a numeric vector `x1`, a "character" vector `x2`, and a "integer" matrix `x3`.

## Section 5.1 Exercises

**Exercise 2** The command below creates a list named `Employees` containing three elements:

- Name, a "character" vector containing the names of three employees
- Salary, a numeric vector containing their salaries
- Union, a "logical" vector indicating whether or not they belong to a union.

```
Employees <- list(
  Name = c("Joe", "Tom", "Ann"),
  Salary = c(50000, 47000, 65000),
  Union = c(FALSE, FALSE, TRUE))
```

a) After creating the `Employees` list, type:

```
Employees
```

and report the results.

b) Use `str()` to look at the structure of the list. Report the results.

c) Use `length()` to find the number of elements in the list. Report the result.

## 5.2 General List Operations

### 5.2.1 Accessing List Elements

- We access elements of a list using double square brackets `[[ ]]`, the dollar sign `$`, or single square brackets `[ ]`:

```
[[ ]]      # Access a list element via its index or name
$         # Access a list element via its name
[ ]      # Access a list element via its index or name, re-
          # turning a list
```

- We almost always use either `[[ ]]` or `$`. The main distinctions are:
  - `[[ ]]` and `$` return the actual *object* from the list. For example, if the list element is a vector, they return a vector.

- `[ ]` doesn't return the actual *object* from the list, but instead returns a *list* containing that object.
  - `[[ ]]` can be used with numerical index values or names of list elements.
  - `$` can only be used with names of list elements.
  - `[ ]` can extract more than one list element, but `[[ ]]` and `$` extract only a single element.
- Here we use double square brackets `[[ ]]` to extract the second element from the list `x` created above:

```
x[[2]]                                # We could also use x[["x2"]]
## [1] "a" "b" "c"
```

Note that a "character" vector is returned. We could also have used `x[["x2"]]`.

- Here we use the dollar sign operator `$` to extract the second element from `x`:

```
x$x2
## [1] "a" "b" "c"
```

A "character" vector is returned here too.

- Now watch what happens when we use single brackets `[ ]` to extract the second element from `x`:

```
x[2]
## $x2
## [1] "a" "b" "c"
```

This time a *list* with one element (the vector `x2`) is returned. This is usually *not* what we want.

### 5.2.2 Adding and Deleting List Elements

- The operators `[[ ]]` and `$` (and also `[ ]`) can be used to add or delete a list element.
- Below, we add the value 16 as the fourth element of `x` (created earlier) and give it the name `x4`:

```
x$x4 <- 16                            # We could also use x[["x4"]] <- 16
x
## $x1
## [1] 1 2 3
##
## $x2
## [1] "a" "b" "c"
##
## $x3
##      [,1] [,2]
## [1,]    1    3
## [2,]    2    4
##
## $x4
## [1] 16
```

Above, we could also have used `x[["x4"]] <- 16`.

- To delete a list element, we set its value to NULL:

```
x$x4 <- NULL
x

## $x1
## [1] 1 2 3
##
## $x2
## [1] "a" "b" "c"
##
## $x3
##      [,1] [,2]
## [1,]    1    3
## [2,]    2    4
```

### Section 5.2 Exercises

**Exercise 3** Recreate the `Employees` list from Exercise 2.

- a) What kind of object (vector or list) will returned by:

```
Employees[[2]]
```

What kind of object (vector or list) will returned by the following command:

```
Employees$Salary
```

What kind of object (vector or list) will returned by:

```
Employees[2]
```

- b) Guess what the result of the following command will be, then check your answer:

```
Employees[[2]][2]
```

Guess what the result of the following command will be, then check your answer:

```
Employees$Salary[2]
```

- c) Guess what the following command does, then check your answer:

```
Employees$YearsExperience <- c(2, 4, 9)
```

Could we have accomplished the same thing by typing the following?:

```
Employees[["YearsExperience"]] <- c(2, 4, 9)
```

### 5.3 Named List Elements

- We can get or add list element names using:

```
names()      # Examine or change the names of list elements
```

- As an example, consider again the list `x`:

```
x
## $x1
## [1] 1 2 3
##
## $x2
## [1] "a" "b" "c"
##
## $x3
##      [,1] [,2]
## [1,]    1    3
## [2,]    2    4
```

To get the list element names, we type:

```
names(x)
## [1] "x1" "x2" "x3"
```

and to change them to, say, `y1`, `y2`, and `y3`, we type:

```
names(x) <- c("y1", "y2", "y3")
names(x)
## [1] "y1" "y2" "y3"
```

- To remove the names, we'd type:

```
names(x) <- NULL
```

### Section 5.3 Exercises

**Exercise 4** Here's a simple list `x`:

```
z <- list(z1 = c(1, 2), z2 = c("a", "b"), z3 = 12)
```

- a) What will the following command return? Check your answer.

```
names(z)
```

- b) What does the following command do? Make sure to check your answer.

```
names(z) <- c("y1", "y2", "y3")
```